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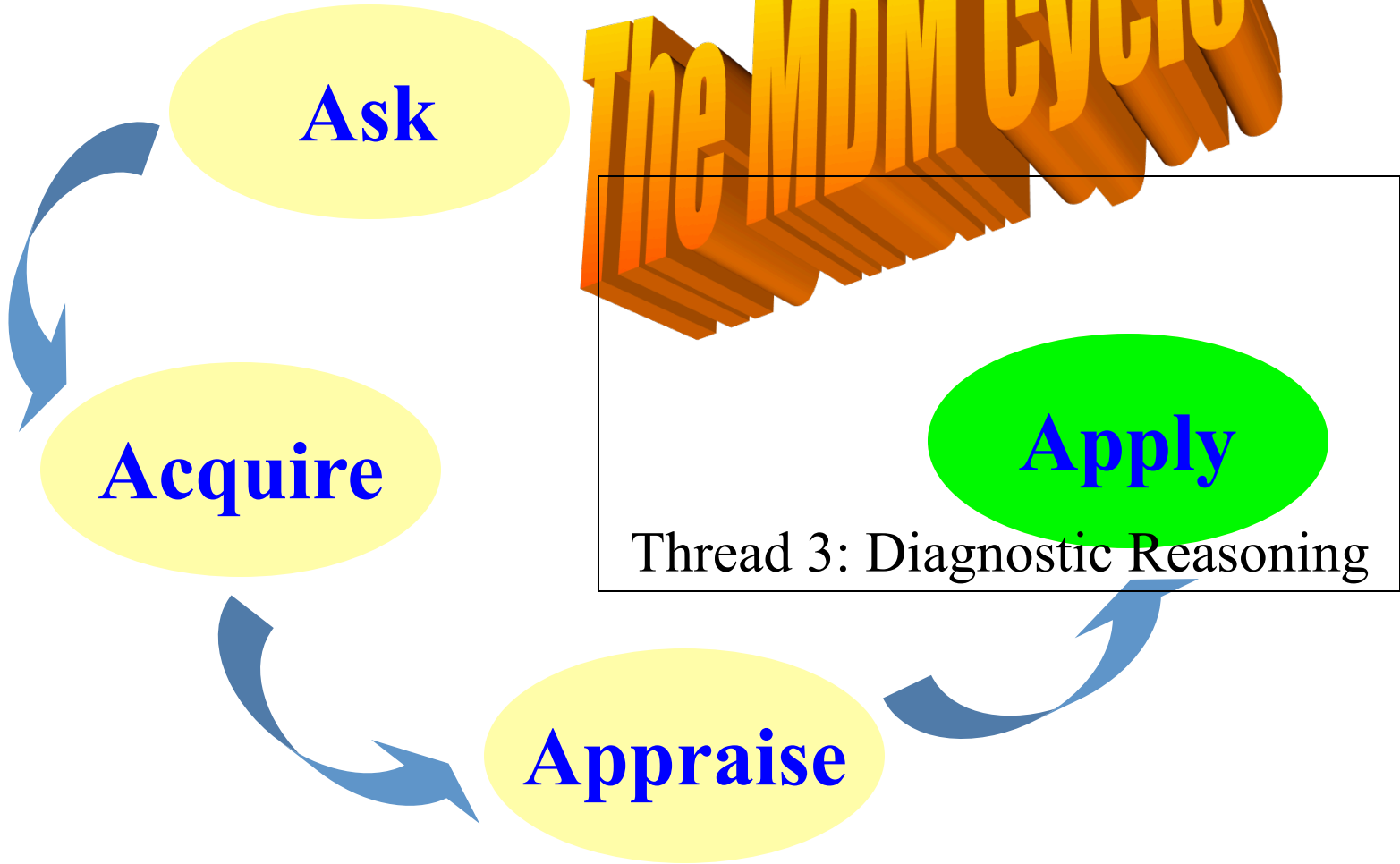
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Patients and Populations

Medical Decision-Making: Diagnostic Reasoning I and II

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The MDM Cycle



Learning Objectives

By the end of this lecture, you will...

- **demonstrate** diagnostic question formulation
- **define** and **calculate** sensitivity, specificity, and predictive values for diagnostic tests
- **explain** how risk factors drive prior probabilities, and how this concept relates to prevalence
- **modify** probabilities from test results through 2x2 table calculations, Bayesian reasoning, and Likelihood Ratios

Case: Diagnostic Reasoning

- The case: A 60 year old man without heart disease presents with sudden onset of shortness of breath.
- Description of the problem: Yesterday, after flying in from California the day before, the patient awoke at 3AM with sudden shortness of breath. His breathing is not worsened while lying down.

Diagnostic Reasoning: Your Intake

- Q: “What other symptoms were you feeling at the time?”
- A: He has had no chest pain, no leg pain, no swelling. He just returned yesterday from a long plane ride. He has no history of this problem before. He takes an aspirin every day. He smokes a pack of cigarettes a day.

Diagnostic Reasoning: First Steps

The *differential diagnosis*

Basic Tasks:

- Assign likelihoods to each possibility
 - E.g. $P(X)$ = probability that “X” is the cause of the patient’s symptoms
- Place the possibilities in descending order of likelihood
- State why (rationale)

My list

My differential diagnosis

- Pulmonary embolism
- Congestive heart failure
- Emphysema exacerbation
- Asthma exacerbation

Probabilities

(1) PE $P(\text{PE}) = 40\%$

(2) CHF $P(\text{CHF}) = 30\%$

(3) Emphysema $P(\text{emphysema}) = 20\%$

(4) Asthma $P(\text{asthma}) = 10\%$

- What is the probability that the shortness of breath is due to either PE or CHF?

Prior Probabilities

- Based on many factors:
 - Clinician experience
 - Patient demographics
 - Characteristics of the patient presentations (history and physical exam)
 - Previous testing
 - Basic science knowledge
- Quite variable but can be standardized
 - Clinical Prediction Rules
 - <http://medcalc3000.com/PulmonaryEmbRiskPisa.htm>

More information

- Family history: he has had a DVT in the past (age 40)
- Physical Exam:
 - His blood oxygen saturation is normal on room air
 - His respiratory rate is 16, but his pulse rate is 105 beats per minute
 - Examination of his lungs reveals some crackles and wheezes, but no pleural rub or evidence of consolidation.
 - Swollen right leg, with firm vein below the knee
- CXR: normal
- EKG: sinus tachycardia

<http://medcalc3000.com/PulmonaryEmbRiskPisa.htm>

Diagnostic Reasoning: Testing

- If a Test existed that could “rule in” PE as the diagnosis with 100% certainty:

then $P(\text{PE} \mid \text{Test}+) = 100\%$

- Two questions:
 - What is this test called?
 - Does $P(\text{CHF} \mid \text{Test}+) = 0\%$?

Diagnostic Testing

- Facilitates the modification of probabilities.
- Can include any/all of the following:
 - Further history taking
 - Physical Examination maneuver
 - Simple testing (laboratory analysis, radiographs)
 - Complex technology (stress testing, angiography, CT/MRI, nuclear scans) \$\$\$

PICO: The Anatomy of a Diagnostic Foreground Question

- D** • Patient: define the clinical condition or **disease** clearly.
- T** • Intervention: define the diagnostic **test** clearly
- G** • Comparison group: define the accepted **gold standard** diagnostic test to compare the results against.
- P** • Outcomes of interest: the outcomes of interest are the properties of the test itself (e.g., **performance** and others we' ll discuss).

Practice PICO

Case: A 60 year old man without heart disease presents with sudden onset of shortness of breath. Considering *PE*.

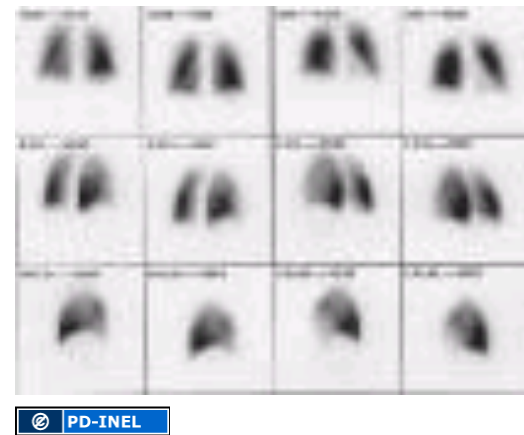
Diagnostic Test to consider:
Ventilation / Perfusion

Scanning

Test: $V/Q +$ means that there

is a HIGH probability of a PE (mismatch between ventilation and perfusion)

$V/Q -$ the probability is NOT high.



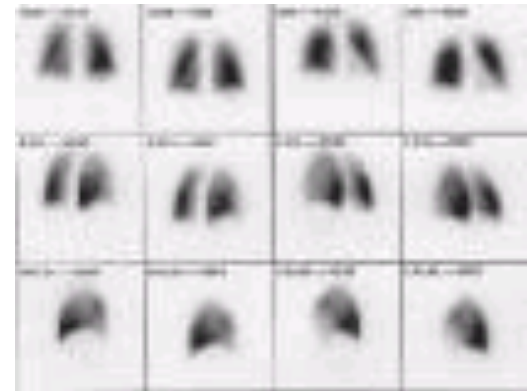
Practice PICO

Case: A 60 year old man without heart disease presents with sudden onset of shortness of breath. Considering *PE*. **P**

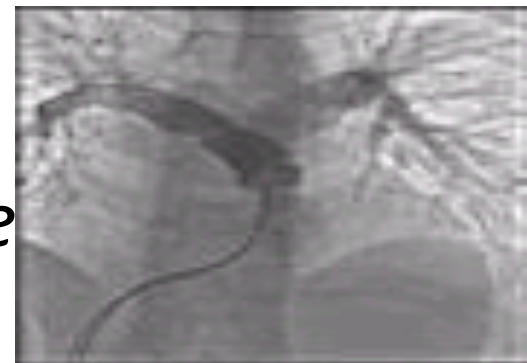
Diagnostic Test to consider:
Ventilation / Perfusion Scanning **I**

Gold standard: *Pulmonary angiography* **C**

Need: *Diagnostic performance* **O**



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Can the test be used?

Step 1 - Accuracy and Precision

- Accuracy - The result of the test corresponds consistently with the true result.
 - The test yields the **correct value**
- Precision - The measure of the test's reproducibility when repeated on the same sample.
 - The test yields the **same value**

Accuracy vs. Precision



High Accuracy
High Precision



Proceed to Step 2



High Precision
Low Accuracy



Calibrate Equipment



High Accuracy
Low Precision



Start Over

Can the test be used?

Step 2 - Diagnostic Performance

1. A well-defined group of people being evaluated for a condition undergo:
 - an experimental test, and
 - the gold standard test.
2. Comparison is made between the result of the new test and that of the gold standard.

Diagnostic Performance: *Statistical* Significance

- Statistical significance: strength of the association between...
 - Diagnostic study results (for the diagnosis of a particular disease)
 - Gold standard results (for the diagnosis of the same disease, in the same population)

- Strength = degree of correlation

Diagnostic Performance: *Clinical* Significance

- Clinical significance: how likely is the diagnostic test going to affect patient care?
 - Magnitude of the association between test results and the accepted gold standard
 - Other literature (including those of the gold standard)
 - Cost of the test, reproducibility of test
 - Disease characteristics (will the test result affect management of the disease?)

What are the results - Diagnosis

Diagnostic performance is an association between test result and diagnosis of a condition (as assessed by the gold standard)

BONUS
What type of variable is disease state?

	Disease +	Disease -
Test +	A TP	B FP
Test -	C FN	D TN

Which test characteristics?

- There are prevalence-dependent and prevalence-independent measures in diagnostic tests.
- Prevalence-independent: sensitivity and specificity.
- Prevalence-dependent: positive and negative predictive values.

Test Characteristics: SeNsitivity

Sensitivity:

- The probability that the test will be positive when the disease is present.

$$P(\text{Test } + \mid \text{Disease } +)$$

- Of all the people WITH the disease, the percentage that will test positive.
- A seNsitive test is one that will detect most of the patients who have the disease (low false-Negative rate).

Test Characteristics: SPecificity

Specificity:

- The probability that the test will be negative when the disease is absent.
 $P(\text{Test -} \mid \text{Disease -})$
- Of all the people WITHOUT the disease, the percentage that will test negative.
- A sPecific test is one that will rarely be positive in patients who don't have the disease (low false-Positive rate).

Test Characteristics: Predictive Values

- Positive predictive value: the probability that a patient has a disease, given a positive result on a test.

$$P(\text{Disease } + \mid \text{Test } +)$$

- Negative predictive value: the probability that a patient does not have a disease, given a negative result on a test.

$$P(\text{Disease } - \mid \text{Test } -)$$

Diagnostic Test Characteristics

- Sens = $A/(A+C)$
- Spec = $D/(B+D)$
- PPV = $A/(A+B)$
- NPV = $D/(C+D)$

	Dx+	Dx-
T+	A	B
T-	C	D
	A+C	B+D

To reflect upon...

Why?

Sensitivity and Specificity

Prevalence-Independent characteristics

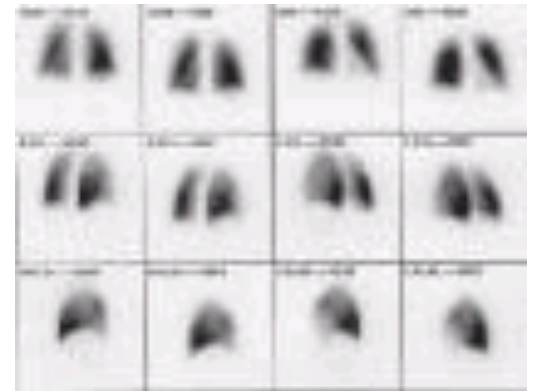
Positive and Negative Predictive Values

Prevalence-Dependent characteristics

Let's try it out

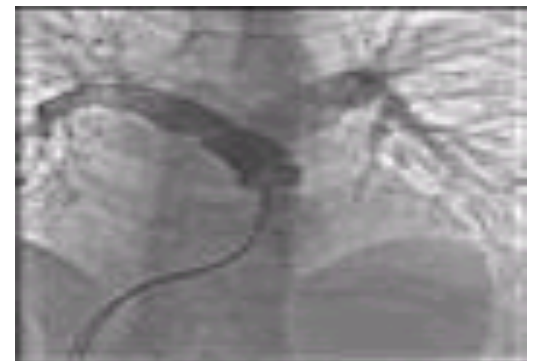
Case: To determine the diagnostic performance of V/Q scans for detecting pulmonary embolism, a study was conducted where 300 patients underwent both a V/Q and pulmonary angiogram. 150 patients were found to have a PE by PA gram. Of those, 75 patients had a **V/Q +** result (high probability). Of the 150 patients without a PE, 125 had a **V/Q -** result.

V/Q scan



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Pulmonary Angiogram



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Let's try it out

Case: To determine the diagnostic performance of V/Q scans for detecting pulmonary embolism, a study was conducted where 300 patients underwent both a V/Q and pulmonary angiogram. 150 patients were found to have a PE by PA gram. Of those, 75 patients had a **V/Q +** result (high probability). Of the 150 patients without a PE, 125 had a **V/Q -** result.

	PE+	PE-
VQ +	75	25
VQ -	75	125
	150	150

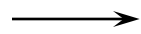
Let's try it out

	PE+	PE-
VQ+	75	25
VQ-	75	125
	150	150

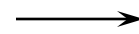
- Sens = $75/(75+75)$
= 50%
- Spec = $125/(125+25)$
= 83%
- PPV = $75/(75+25)$
= 75%
- NPV = $125/(125+75)$
= 63%

Modification of Probability

**Pretest
Probability
 $P(\text{Disease})$**



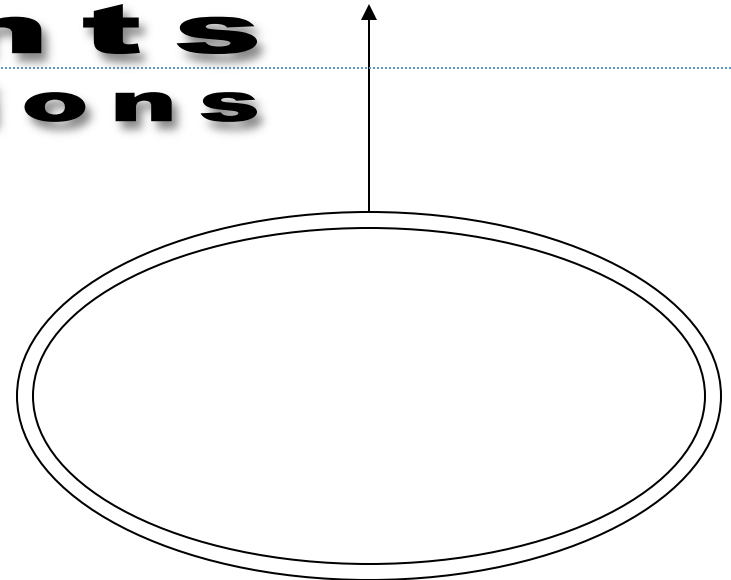
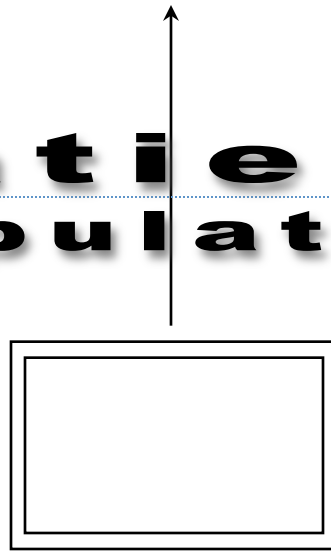
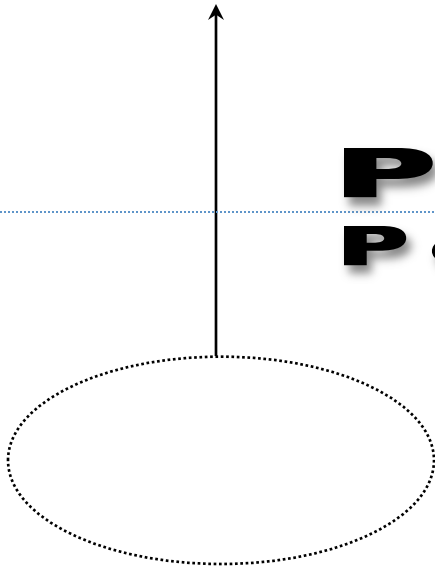
**Test
Result**



**Test result
changes the
probability of
disease**

$P(\text{Disease}|\text{Test Result})$

Patients
Populations



Test Characteristics and Prevalence

- Sens = $A/(A+C)$
- Spec = $D/(B+D)$
- PPV = $A/(A+B)$
- NPV = $D/(C+D)$

	Dx+	Dx-
T+	A	B
T-	C	D
	A+C	B+D

Disease Prevalence

Prevalence

	PE+	PE-
VQ +	75	25
VQ -	75	125
	150	150

- Sens = 50%
- Spec = 83%
- PPV = 75%
- NPV = 63%
- Prevalence = ? **50%**

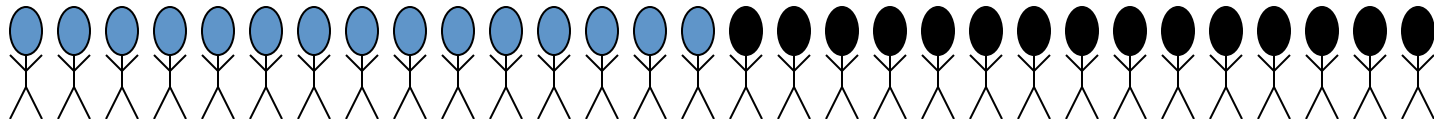
Populations and Patients

Population view

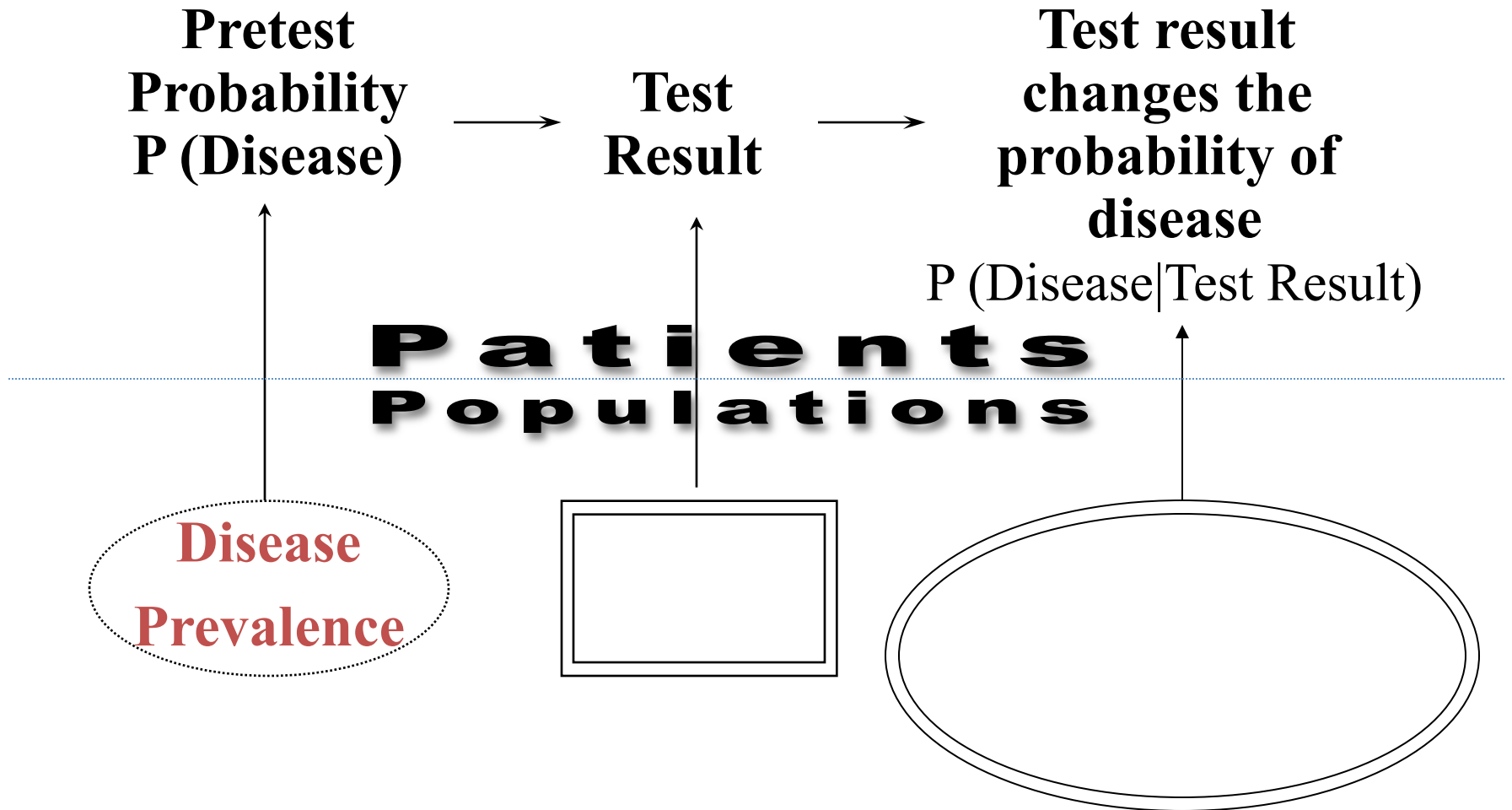
- Prevalence reflects the number of people with the disease at a given moment

Patient view

- Same concept implies how likely an individual patient has the disease
- $P(\text{Disease})$



Modification of Probability



An Important Question and Assumption

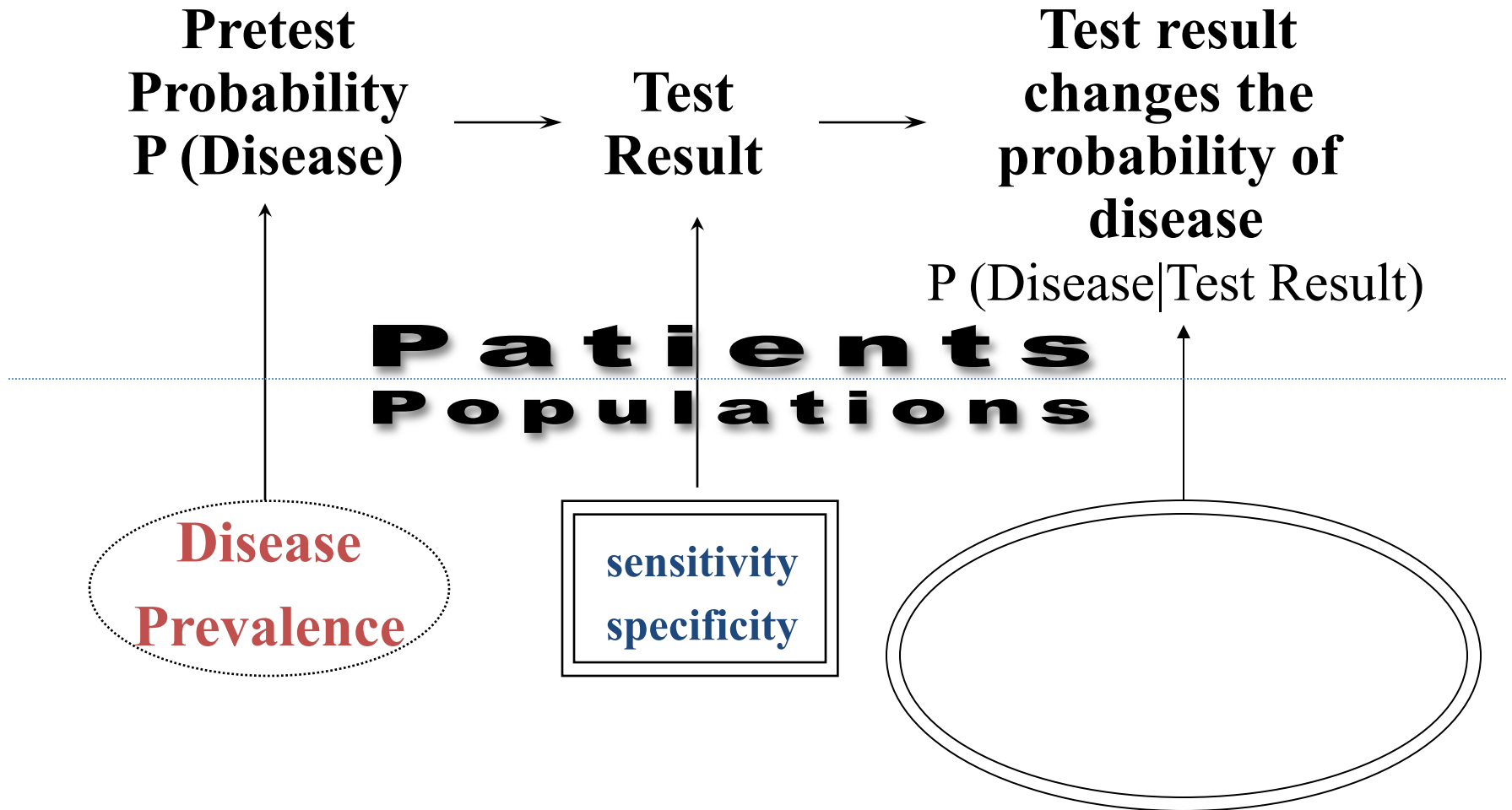
Question: Are certain test characteristics fixed?

Answer: Generally, yes.

Sensitivity and specificity are constants, regardless of the prevalence of the disease in the studied population (prevalence-INdependent)*

*Exceptions and caveats to this assumption are real, but are beyond the scope of this course

Modification of Probability



Importance of Pre-Test Probability

- $V/Q +$ Sens = 50%, Spec = 83%

	Post-TP			
Pre-TP/Prev	PPV	NPV		
50%	75%	63%		

	D+	D-
T+	75	25
T-	75	125

How do our predictive values relate to our probability after the test result is obtained (our post-test probabilities)?

Importance of Pre-Test Probability

- V/Q + Sens = 50%, Spec = 83%

	Post-TP		
Pre-TP/Prev	PPV	NPV	
50%	75%	63%	

	D+	D-
T+	75	25
T-	75	125

- If our Pre-test Probability was 50%, and we obtain a V/Q + scan on this patient, what is our Post-test probability?

Importance of Pre-Test Probability

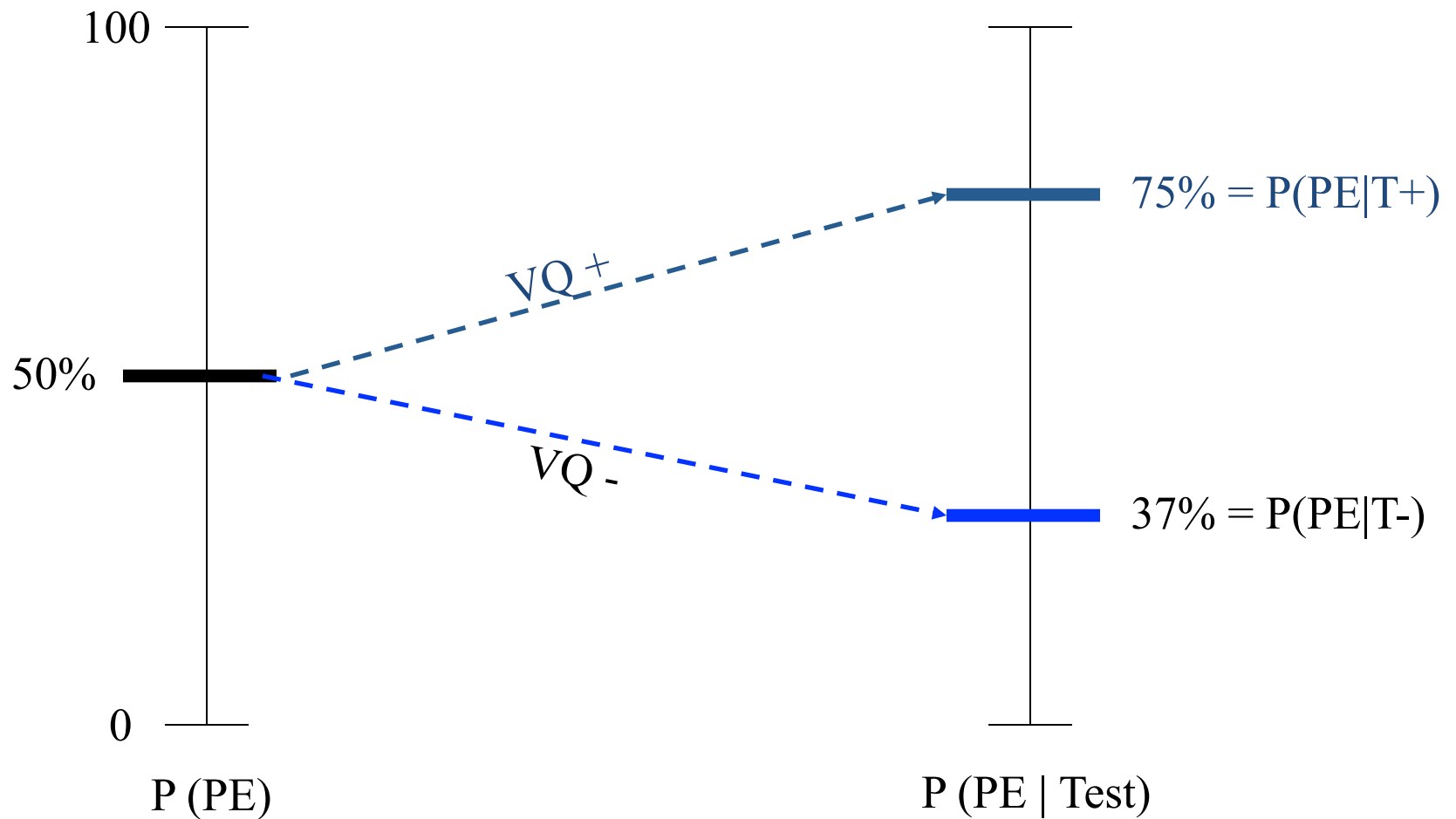
- V/Q + Sens = 50%, Spec = 83%

	Post-TP		
Pre-TP/Prev	PPV	NPV	
50%	75%	63%	

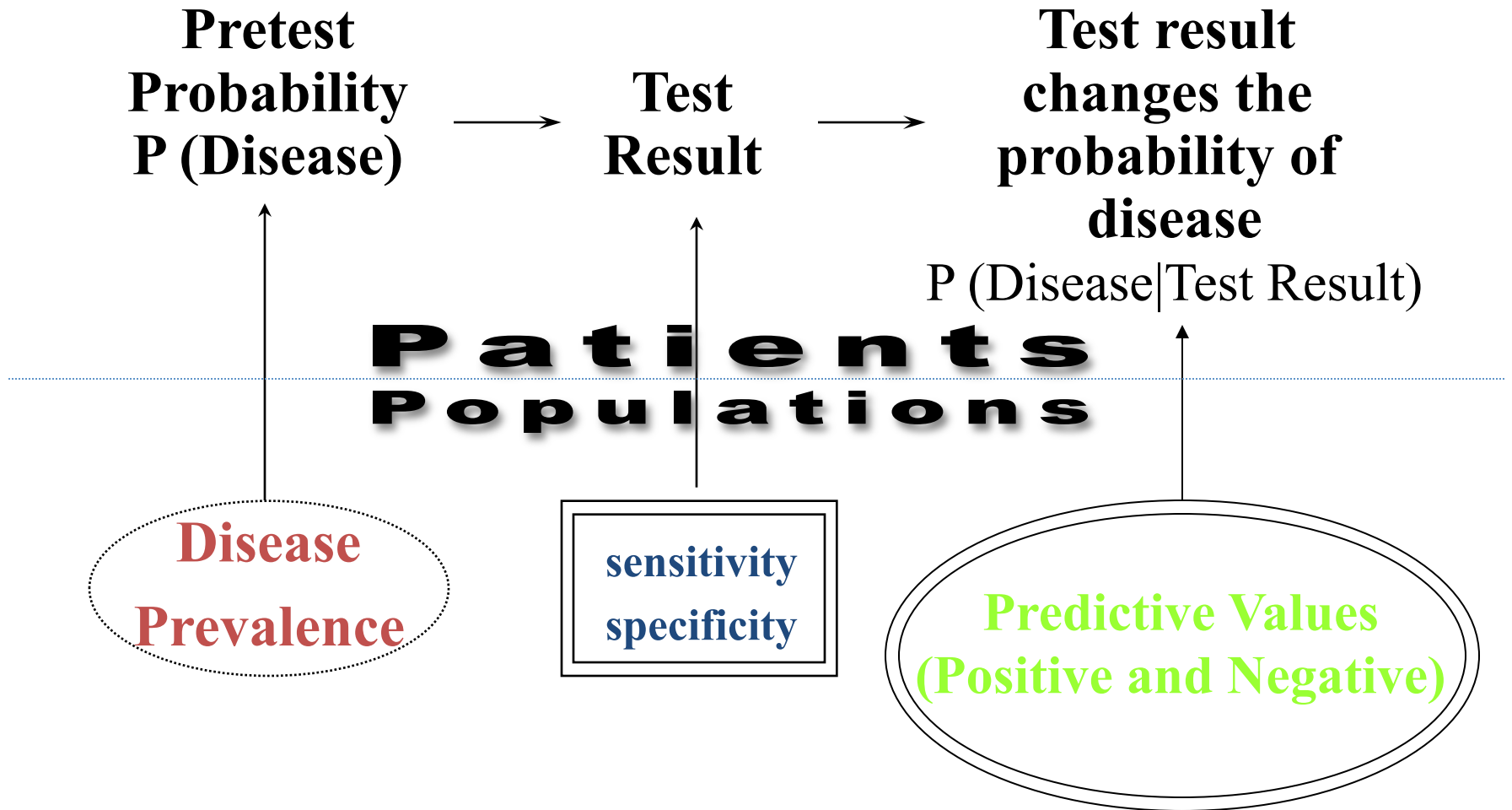
	D+	D-
T+	75	25
T-	75	125

- If our Pre-test Probability was 50%, and we obtain a V/Q – scan on this patient, what is our Post-test probability?

What did we just do?



Modification of Probability



Fundamental Assumptions

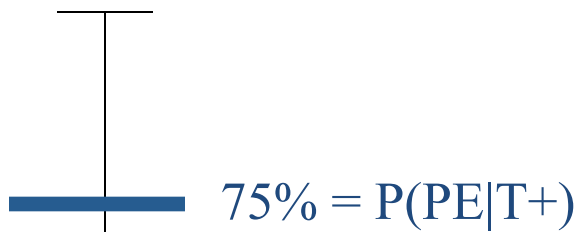
Sensitivity and specificity are constants, regardless of the prevalence of the disease in the studied population (prevalence-INdependent)*

Positive and Negative Predictive Values are dependent on the prevalence of the disease in the studied population (prevalence-DEpendent)

*with exceptions

Now, what do we do?

*clickers



Q1: Choices:

- a) Treat as if patient has PE
- b) Decide to get another test
- c) Decide that patient does not have a PE

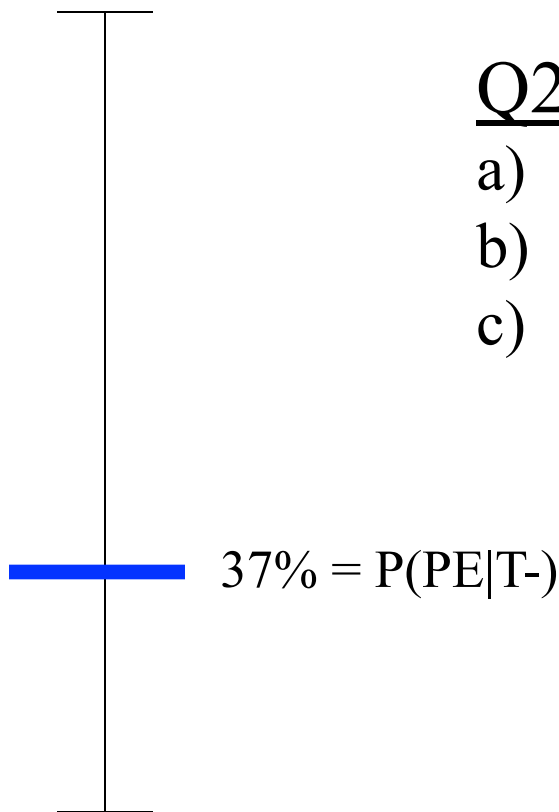
What factors do you consider when making the next decision?

Now, what do we do?

*clickers

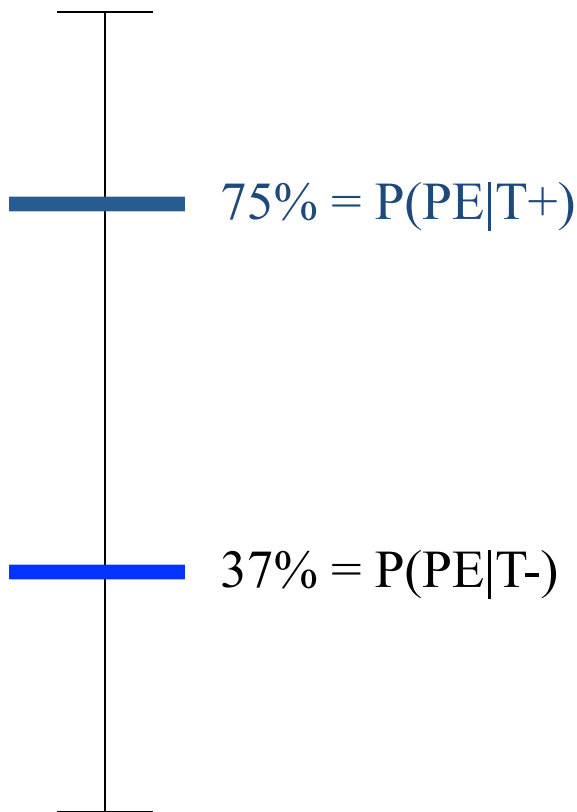
Q2: Choices:

- a) Treat as if patient has PE
- b) Decide to get another test
- c) Decide that patient does not have a PE



What factors do you consider when making the next decision?

Now, what do we do?



Choices:

- Treat as if patient has PE
- Decide to get another test
- Decide that patient does not have a PE

Choices:

- Treat as if patient has PE
- Decide to get another test
- Decide that patient does not have a PE

What factors do you consider when making the next decision?

What if we change our pretest probability?

- In essence, we are simultaneously changing the prevalence:
 - Original pre-TP = $P(PE) = 50\%$ HIGH RISK
 - New pre-TP = $P(PE) = 25\%$ MED RISK
- Assuming that sensitivity and specificity are fixed...then we must recalculate our predictive values to determine our new post-test probabilities.

Importance of Pre-Test Probability

- V/Q + Sens = 50%, Spec = 83%

Pre-TP/Prev	Post-TP	
	PPV	NPV
hi risk 50%	75%	63%
med risk 25%	50%	83%
	$38/(38+38)$	$187/(187+37)$

	D+	D-
T+	75	25
T-	75	125

	D+	D-
T+	38	38
T-	37	187

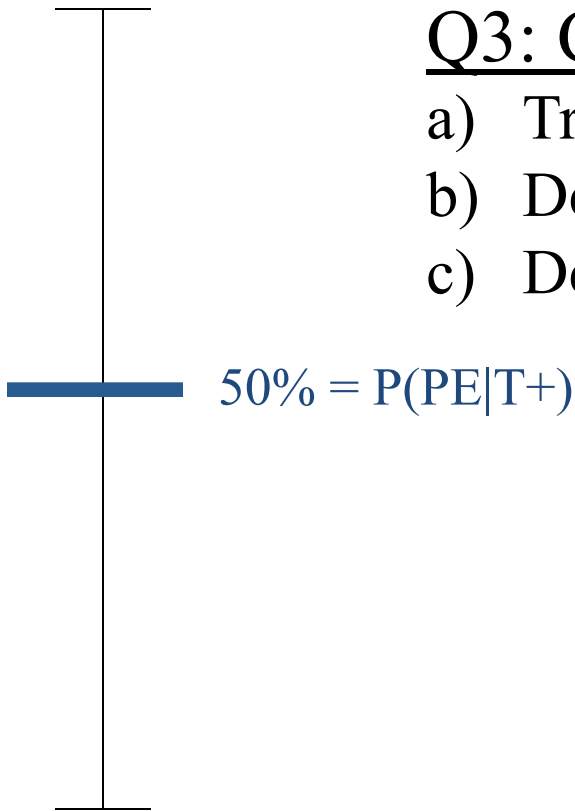
Our Pre-test Probability was 25%, we obtain a V/Q – scan on this patient, our Post-test probability is now...

Decision time

*clickers

Q3: Choices:

- a) Treat as if patient has PE
- b) Decide to get another test
- c) Decide that patient does not have a PE

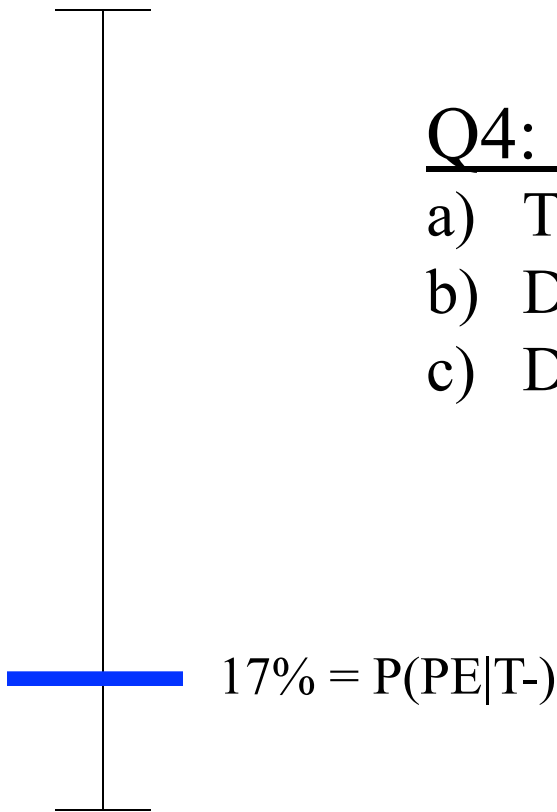


Decision time

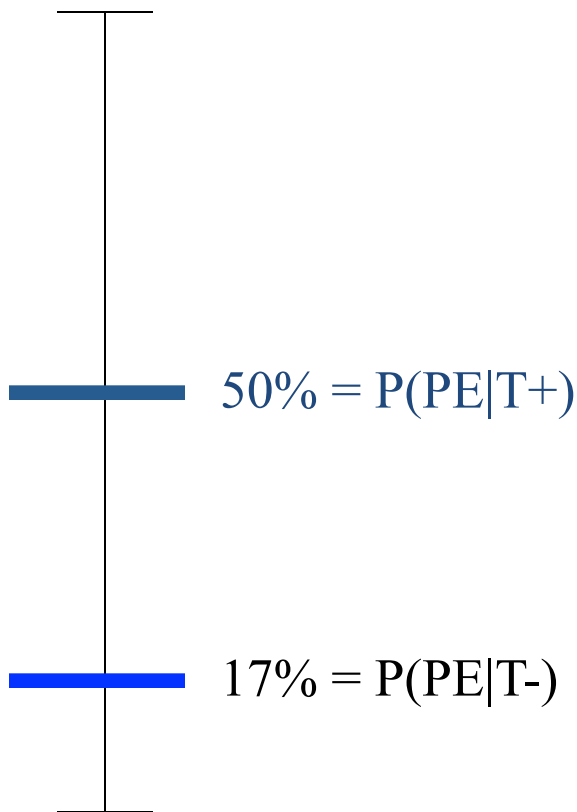
*clickers

Q4: Choices:

- a) Treat as if patient has PE
- b) Decide to get another test
- c) Decide that patient does not have a PE



Decision time



Choices:

- Treat as if patient has PE
- Decide to get another test
- Decide that patient does not have a PE

Choices:

- Treat as if patient has PE
- Decide to get another test
- Decide that patient does not have a PE

Let's change it again...

- Again, we are changing the prevalence:
 - Young woman, no risk factors, some dyspnea, no history, normal exam
 - If we consult our clinical prediction rule:
 - New pre-TP = $P(\text{PE}) = 5\%$: LOW RISK

Importance of Pre-Test Probability

- V/Q + Sens = 50%, Spec = 83%

		Pred Val			
Pre-TP/Prev		PPV	NPV	T+	T-
hi risk	50%	75%	63%	75	25
lo risk	5%	15%	97%	75	125
		$8/(8+47)$	$238/(238+7)$		

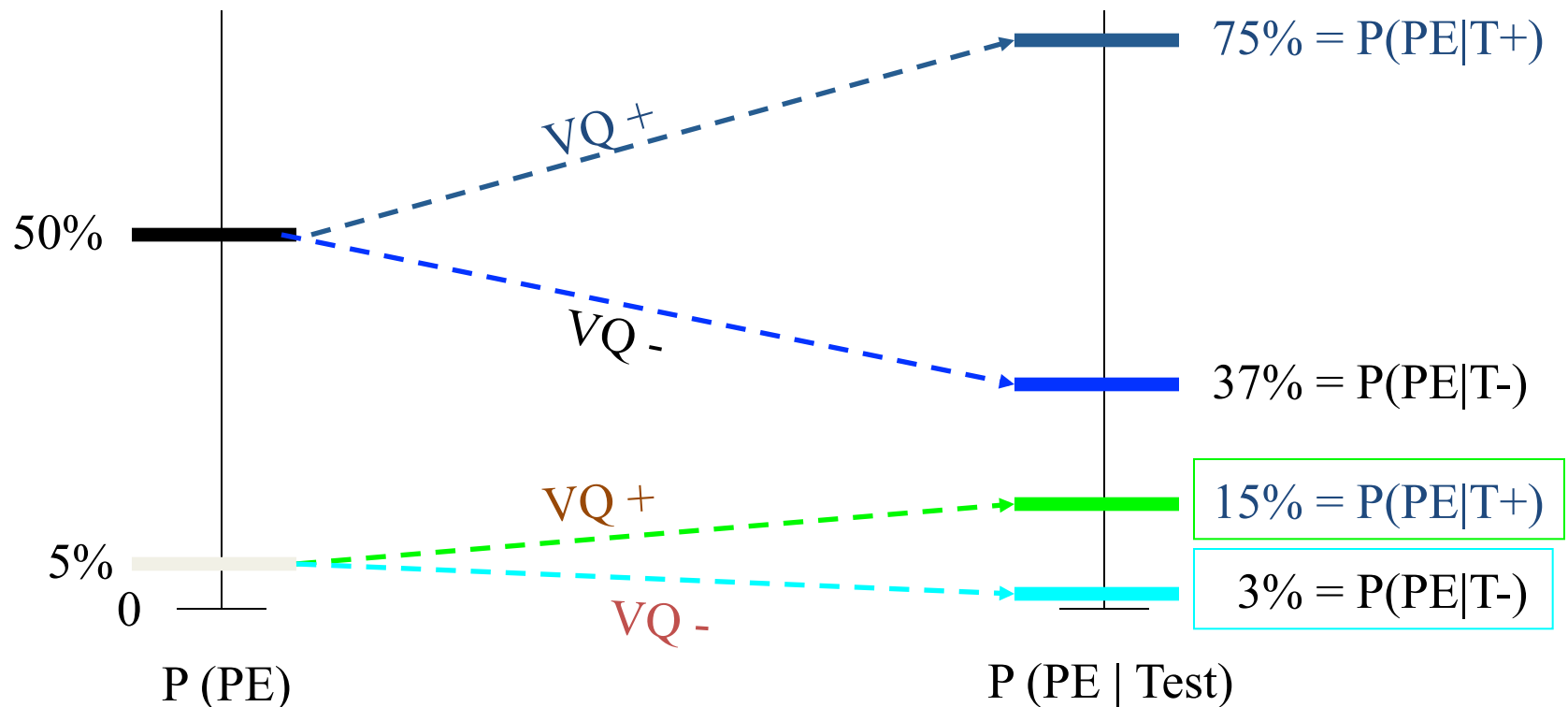
	D+	D-
T+	75	25
T-	75	125

	D+	D-
T+	8	47
T-	7	238

What did we just do?

Observation

As prevalence (pre-test probability) decreases, positive tests are more likely to be false-positives



Fundamentally...

Question: If you get a **V/Q +** scan for the diagnosis of pulmonary embolism, is it more likely to represent a false positive test if the patient presented with...

- (a) many clinical features of PE (shortness of breath, chest pain, long plane ride), or
- (b) no clinical features of PE (no shortness of breath, no chest pain, no leg swelling, no long plane ride)?

Alternative Vocabulary - Rates

- True Positive Rate = sensitivity
- False Positive Rate = 1-specificity
- False Negative Rate = 1-sensitivity
- True Negative Rate = specificity

Combining Rates - Methods

- Likelihood Ratios
- ROC Curves

Combining Rates - Method 1

Likelihood Ratios (LR)

- Concept - LRs depict the relationship between true and false rates
 - $\text{TPR}/\text{FPR} = \text{LR}$ for a positive test result
 - $\text{FNR}/\text{TNR} = \text{LR}$ for a negative test result

$$\text{LR} = \frac{\text{TPR}}{\text{FPR}} = \frac{\text{sens}}{1-\text{spec}}$$

Typically >1 , excellent >10

$$\text{LR} = \frac{\text{FNR}}{\text{TNR}} = \frac{1-\text{sens}}{\text{spec}}$$

Typically <1 , excellent <0.1

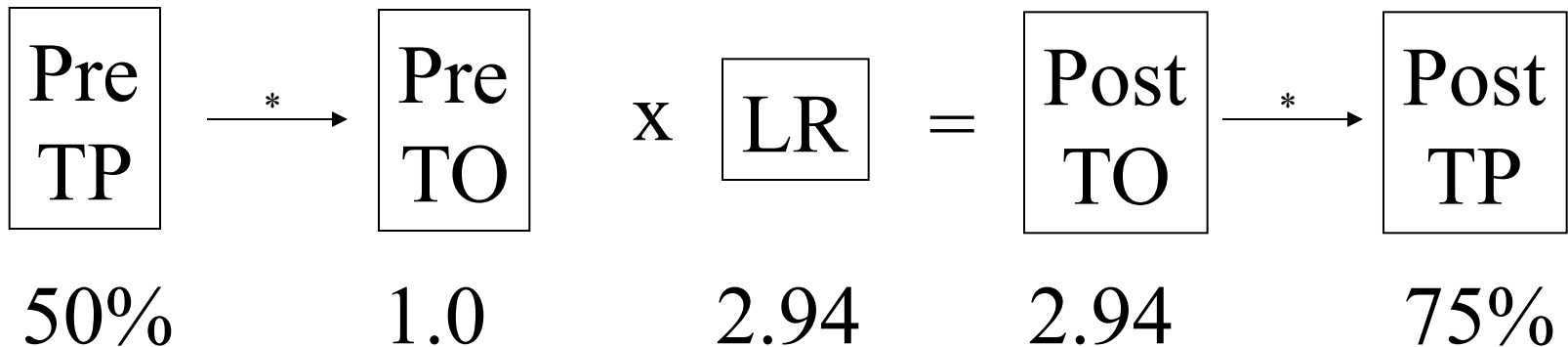
Application

Likelihood Ratios (LR)

Key Concept: LRs can be combined with pre-test odds to get post-test odds

Remember our scenario:
High risk pt - 50% (PreTP)
0.50

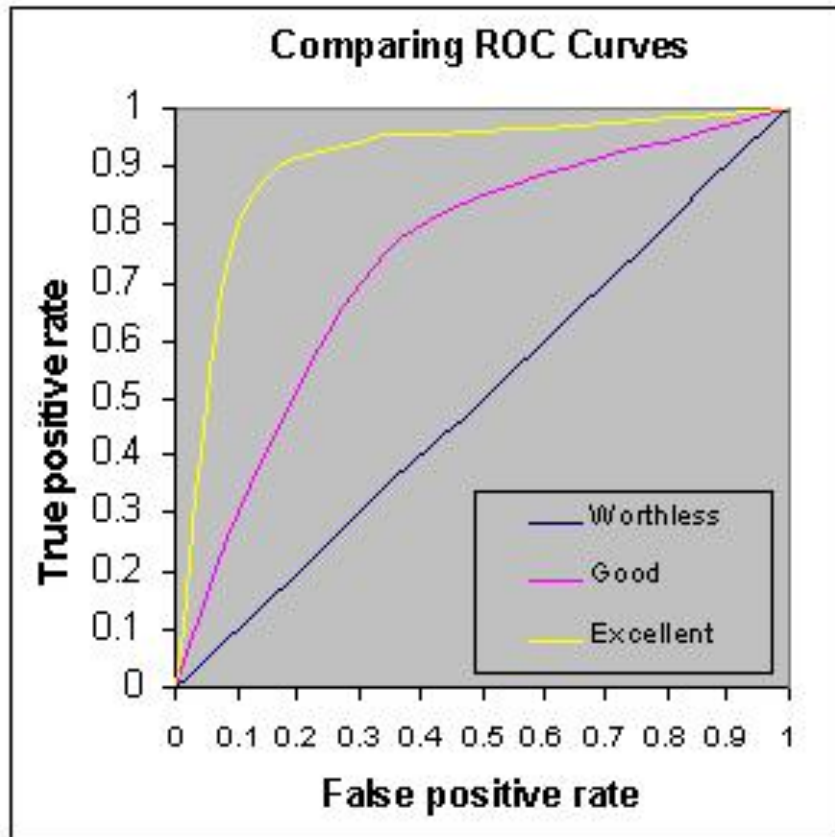
$$\text{LR (VQ hi)} = \frac{\text{-----}}{1-0.83} = 2.94$$



*converting odds to probability and vice and versa - many references online

Combining Rates - Method 2

ROC Curves



Visual depiction of LR

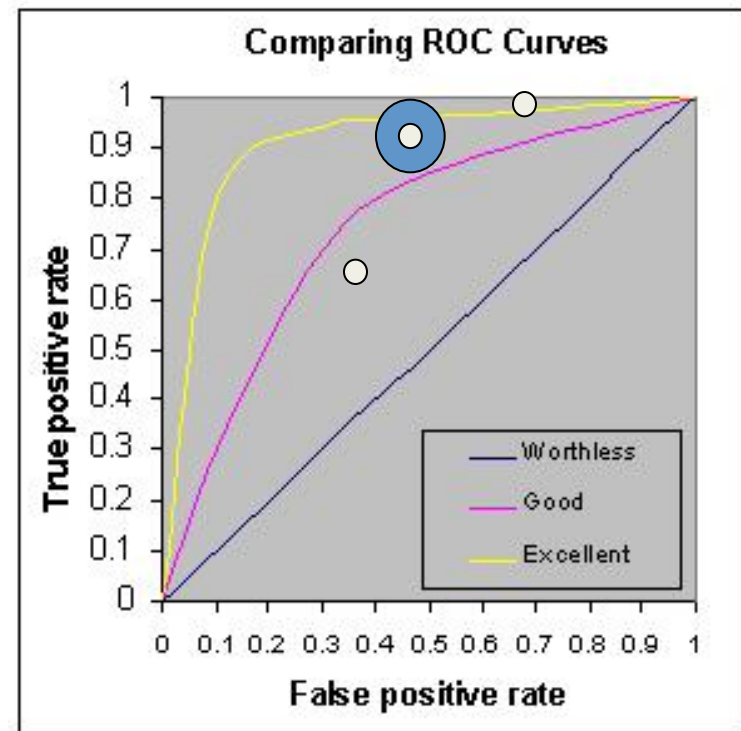
- Tests with continuous values only
- Sensitivity-specificity tradeoff at different cutoffs
- TPR plotted against FPR

Application

ROC Curves

ROC Curves

- Area under the curve determines overall utility of the test
- Inflection point reflects optimal threshold
- More in Small Group Exercise
 - Assignment 3



Take Home Points

- Research studies of diagnostic tests give you test characteristics, not predictive values.
- Relationships between sensitivity and specificity can be captured in ROC curves (for tests with thresholds) and Likelihood Ratios (LRs)
- Appropriate use of tests stem from large differences between pre-test and post-test probabilities, resulting from LR's that strongly deviate from 1.
- If your pre-test probability is very low (<10%) or very high (>90%), it is rare that a single test can help.

The Odyssey: Conclusion



Initial Possibilities

- #1: Trunk latch defect (recall pending)
- #2: Ajar sensing defect on side door
- #3: Side door not closing properly



The Answer

- #2: Ajar sensing defect on side door

Initial Diagnostic Reasoning

The Odyssey Reloaded

The Mechanic

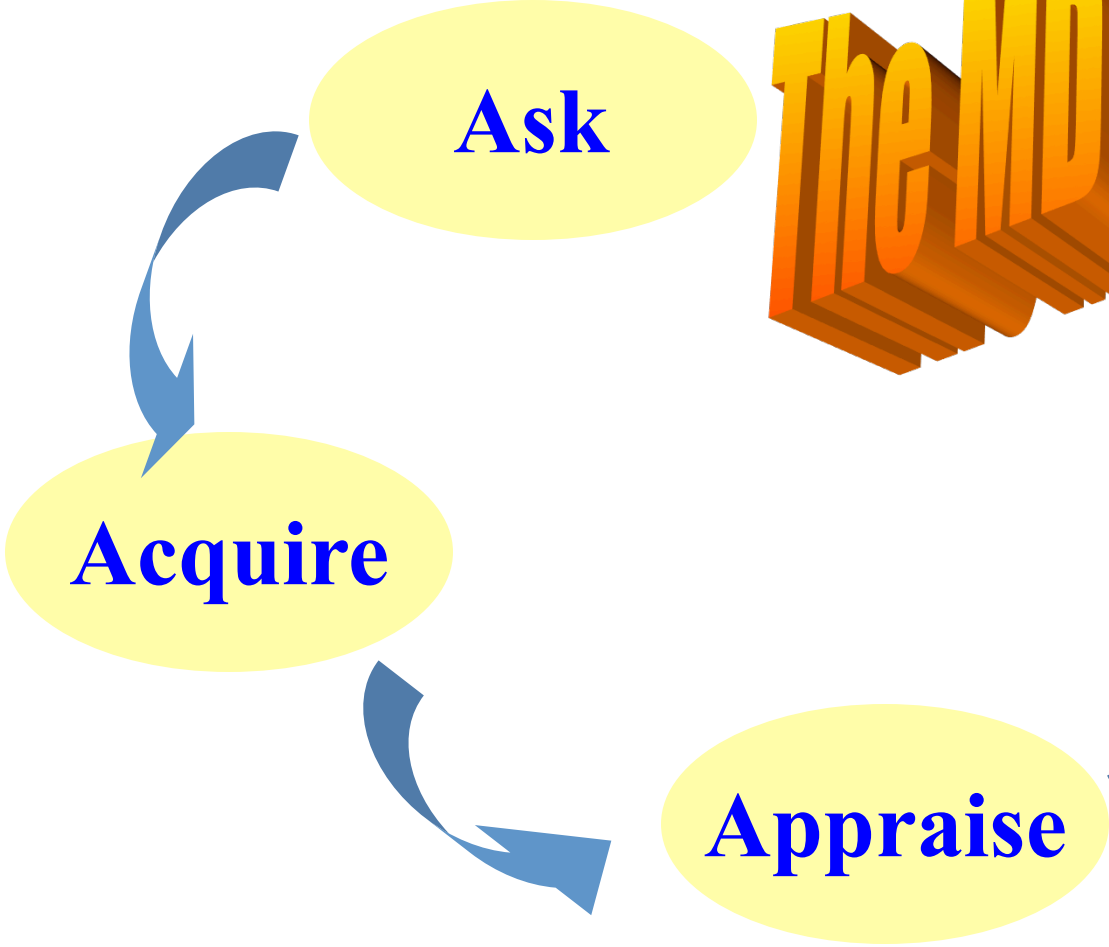


The Clinician

- Failure to entertain all possibilities
- Failure to pay attention to all symptoms
- Failure to inform customer
- Failure to perform diagnostic tests

- Entertain all important possibilities
- Elicit and pay attention to description of all symptoms
- Inform and involve patients
- **Perform effective diagnostic tests**

The MDM Cycle



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